





2. A car has mass 1200 kg. The maximum power of the car's engine is 32 kW. The resistance to motion due to non-gravitational forces is modelled as a force of constant magnitude 800 N. When the car is travelling on a horizontal road at constant speed  $V \text{ m s}^{-1}$ , the engine of the car is working at maximum power.

- (a) Find the value of  $V$ . (3)

The car now travels downhill on a straight road inclined at an angle  $\theta$  to the horizontal, where  $\sin \theta = \frac{1}{40}$ . The resistance to motion due to non-gravitational forces is still modelled as a force of constant magnitude 800 N. Given that the engine of the car is again working at maximum power,

- (b) find the acceleration of the car when its speed is  $20 \text{ m s}^{-1}$ . (4)

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3 A particle *P* of mass 0.25 kg moves under the action of a single force **F** newtons. At time *t* seconds, the velocity of *P* is **v** m s<sup>-1</sup>, where

$$\mathbf{v} = (2 - 4t)\mathbf{i} + (t^2 + 2t)\mathbf{j}$$

When *t* = 0, *P* is at the point with position vector  $(2\mathbf{i} - 4\mathbf{j})$  m with respect to a fixed origin *O*. When *t* = 3, *P* is at the point *A*. Find

(a) the momentum of *P* when *t* = 3, (2)

(b) the magnitude of **F** when *t* = 3, (6)

(c) the position vector of *A*. (5)

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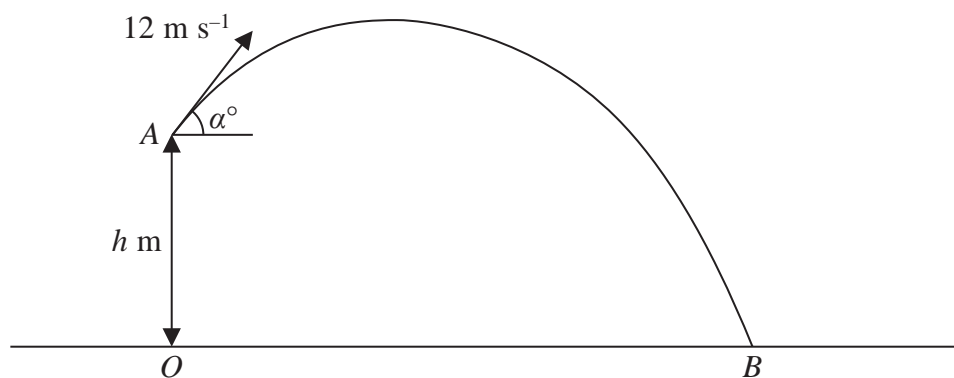


Figure 1

The points  $O$  and  $B$  are on horizontal ground. The point  $A$  is  $h$  metres vertically above  $O$ . A particle  $P$  is projected from  $A$  with speed  $12 \text{ m s}^{-1}$  at an angle  $\alpha^\circ$  to the horizontal. The particle moves freely under gravity and hits the ground at  $B$ , as shown in Figure 1. The speed of  $P$  immediately before it hits the ground is  $15 \text{ m s}^{-1}$ .

(a) By considering energy, find the value of  $h$ . (4)

Given that  $1.5 \text{ s}$  after it is projected from  $A$ ,  $P$  is at a point  $4 \text{ m}$  above the level of  $A$ , find

(b) the value of  $\alpha$ , (3)

(c) the direction of motion of  $P$  immediately before it reaches  $B$ . (3)

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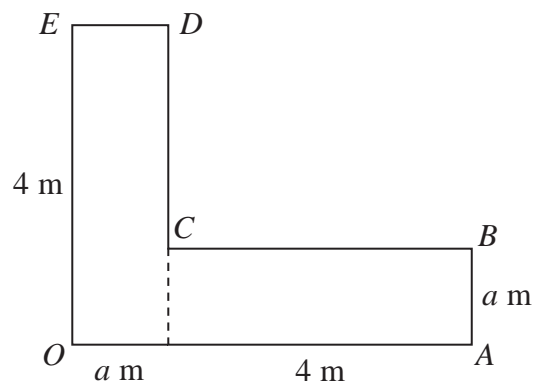
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5.



**Figure 2**

The uniform L-shaped lamina  $OABCDE$ , shown in Figure 2, is made from two identical rectangles. Each rectangle is 4 metres long and  $a$  metres wide. Giving each answer in terms of  $a$ , find the distance of the centre of mass of the lamina from

(a)  $OE$ , (4)

(b)  $OA$ . (4)

The lamina is freely suspended from  $O$  and hangs in equilibrium with  $OE$  at an angle  $\theta$  to the downward vertical through  $O$ , where  $\tan \theta = \frac{4}{3}$ .

(c) Find the value of  $a$ . (4)

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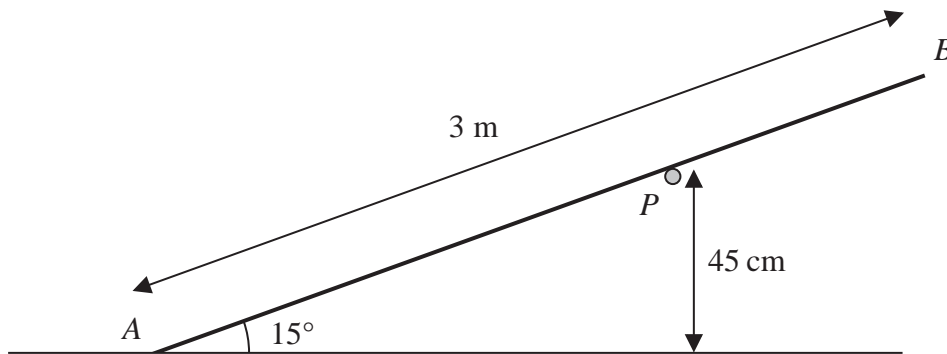


Figure 3

A uniform rod  $AB$  has weight 30 N and length 3 m. The rod rests in equilibrium on a rough horizontal peg  $P$  with its end  $A$  on smooth horizontal ground. The rod is in a vertical plane perpendicular to the peg. The rod is inclined at  $15^\circ$  to the ground and the point of contact between the peg and the rod is 45 cm above the ground, as shown in Figure 3.

- (a) Show that the normal reaction at  $P$  has magnitude 25 N. (4)
- (b) Find the magnitude of the force on the rod at  $A$ . (4)

The coefficient of friction between the rod and the peg is  $\mu$ .

- (c) Find the range of possible values of  $\mu$ . (4)

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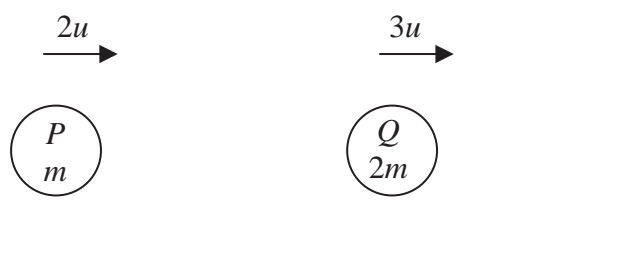


Figure 4

Two smooth particles  $P$  and  $Q$  have masses  $m$  and  $2m$  respectively. The particles are moving in the same direction in the same straight line, on a smooth horizontal plane, with  $Q$  in front of  $P$ . The particles are moving towards a fixed smooth vertical wall which is perpendicular to the direction of motion of the particles, as shown in Figure 4. The speed of  $P$  is  $2u$  and the speed of  $Q$  is  $3u$ . The coefficient of restitution between  $Q$  and the wall is  $\frac{1}{3}$ . Particle  $Q$  strikes the wall, rebounds and then collides directly with  $P$ . The direction of motion of each particle is reversed by this collision. Immediately after this collision the speed of  $P$  is  $v$  and the speed of  $Q$  is  $w$ .

(a) Show that  $v = 2w$ . (5)

The total kinetic energy of  $P$  and  $Q$  immediately after they collide is half the total kinetic energy of  $P$  and  $Q$  immediately before they collide.

(b) Find the coefficient of restitution between  $P$  and  $Q$ . (8)

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